

## Problem A. Bipartite Graph Matching Problem

Input file: *standard input*  
Output file: *standard output*  
Time limit: 2 seconds  
Memory limit: 1024 mebibytes

You are given a bipartite graph. The left part contains  $n_1$  vertices numbered from 1 to  $n_1$ , and the right part contains  $n_2$  vertices numbered from 1 to  $n_2$ . There are  $m$  edges, each connecting one vertex on the left to one vertex on the right.

For every interval  $[\ell, r]$  on the right side (where  $1 \leq \ell \leq r \leq n_2$ ), consider the subgraph obtained by:

- keeping all left vertices  $1, 2, \dots, n_1$ ;
- keeping only the right vertices with numbers in  $[\ell, r]$ ;
- keeping only edges whose endpoints are both kept.

In this subgraph, compute the size of a maximum matching (the maximum number of pairwise disjoint edges). Let this value be denoted by  $f(\ell, r)$ .

You need to compute the following value:

$$\sum_{1 \leq \ell \leq r \leq n_2} f(\ell, r) \cdot \ell \cdot r \cdot ((\ell \oplus r) + 1),$$

where  $\oplus$  denotes the bitwise XOR operation.

Output the value of this sum modulo 998 244 353.

### Input

The first line contains a single integer  $t$  ( $1 \leq t \leq 2000$ ), the number of test cases. For each test case:

The first line contains three integers:  $n_1$ ,  $n_2$ , and  $m$  ( $1 \leq n_1, n_2 \leq 5000$ ,  $1 \leq m \leq 10^4$ ), representing the number of vertices on the left, the number of vertices on the right, and the number of edges.

Each of the next  $m$  lines contains two integers,  $u$  and  $v$  ( $1 \leq u \leq n_1$ ,  $1 \leq v \leq n_2$ ), which describe an edge between left vertex  $u$  and right vertex  $v$ .

There are no multiple edges. The sum of  $n_1$  does not exceed 5000. The sum of  $n_2$  also does not exceed 5000.

### Output

For each test case, output a single line containing one integer: the required sum modulo 998 244 353.

## Example

<i>standard input</i>	<i>standard output</i>
4	81
3 3 5	529
1 1	12
2 1	81
2 2	
2 3	
3 3	
3 4 6	
1 2	
1 4	
2 3	
2 1	
3 4	
3 3	
2 2 1	
1 2	
4 3 5	
1 3	
2 1	
3 3	
4 2	
4 1	

## Problem B. Travelling

Input file: *standard input*  
Output file: *standard output*  
Time limit: 1 second  
Memory limit: 1024 mebibytes

There are  $n$  cities, numbered from 1 to  $n$ . There are also  $n - 1$  bidirectional roads connecting these cities, so that for every two cities  $x$  and  $y$ , there exists a path from  $x$  to  $y$ . The  $i$ -th road connects cities  $u_i$  and  $v_i$ , and has a cost  $c_i$ . Every time you pass through road  $i$ , you spend  $c_i$  coins.

You are now at city 1 and want to travel to visit all cities. Every second, if you are at city  $x$ , you can choose a city  $y$  that is directly connected with city  $x$  by a road, move to city  $y$ , and pay the cost of the respective road. Each road can be passed **at most twice**. When you have visited all cities and are at city 1, you can finish your travel. The cost of the travel is the total cost of all the moves you made.

There is also an integer  $k$ . During your travel, you can use a free coupon once, making your following  $k$  moves have no cost.

For every  $k$  from 0 to  $2n - 2$ , you should calculate the minimum cost of a travel that visits all cities and uses the coupon optimally.

### Input

The first line contains a single integer  $t$  ( $1 \leq t \leq 400$ ), the number of test cases. For each test case:

The first line contains an integer  $n$  ( $1 \leq n \leq 2000$ ), denoting the number of cities.

The next  $n - 1$  lines describe the roads. The  $i$ -th of these lines contains three integers,  $u_i$ ,  $v_i$ , and  $c_i$  ( $1 \leq u_i, v_i \leq n$ ,  $0 \leq c_i \leq 10^9$ ), denoting the cities connected by the  $i$ -th road and the cost of that road.

There is a path between any pair of cities. The sum of  $n$  does not exceed 2000.

### Output

For each test case, output one line containing  $2n - 1$  integers: the answers for  $k$  from 0 to  $2n - 2$ .

### Example

<i>standard input</i>	<i>standard output</i>
2	18 15 12 10 8 5 3 2 0
5	32 27 22 21 17 13 12 8 4 3 2 1 0
1 2 2	
2 3 3	
2 4 1	
4 5 3	
7	
1 2 1	
1 3 1	
1 4 4	
3 5 5	
3 6 1	
6 7 4	

### Note

In the first test case, we can always travel along the path 1, 2, 3, 2, 4, 5, 4, 2, 1, with the cost sequence 2, 3, 3, 1, 3, 3, 1, 2. The cost-free segments for each  $k$  are shown below.

<b>k</b>	<b>cost-free segment</b>	<b>answer</b>
0	$\square$	18
1	[3]	15
2	[3, 3]	12
3	[2, 3, 3]	10
4	[3, 3, 1, 3]	8
5	[3, 3, 1, 3, 3]	5
6	[2, 3, 3, 1, 3, 3]	3
7	[2, 3, 3, 1, 3, 3, 1]	2
8	[2, 3, 3, 1, 3, 3, 1, 2]	0

## Problem C. Stonebag

Input file: *standard input*  
Output file: *standard output*  
Time limit: 3 seconds  
Memory limit: 1024 mebibytes

You are given  $n$  piles of stones, labeled by integers from 1 to  $n$ . The  $i$ -th pile initially contains  $a_i$  stones. You also have a bag, which is initially empty.

You may perform the following operations, any number of times, in any order:

- Choose a pile that is not empty, remove **one** stone from this pile, and put it into the bag.
- Choose a pile (possibly empty), remove **exactly**  $n$  stones from the bag, and put all these  $n$  stones into the chosen pile. This operation can be performed only when the bag contains at least  $n$  stones.

You may stop performing operations at any time. In the end, the bag may contain any (possibly nonzero) number of stones.

Determine how many distinct final configurations of the  $n$  piles can be obtained from the initial configuration by performing a finite sequence of operations. Output the answer modulo 998 244 353.

Two final configurations are considered different if there exists some index  $i$  such that the number of stones in pile  $i$  differs between them. Recall that the piles are labeled and their order matters.

### Input

The first line contains a single integer  $n$  ( $1 \leq n \leq 3000$ ), the number of piles.

The second line contains  $n$  integers  $a_1, a_2, \dots, a_n$  ( $0 \leq a_i \leq 10^9$ ), where  $a_i$  is the initial number of stones in the  $i$ -th pile.

### Output

Output a single integer: the number of distinct final configurations of the piles that can be obtained, modulo 998 244 353.

### Examples

<i>standard input</i>	<i>standard output</i>
2 1 3	15
3 2 1 3	83
8 4 3 6 5 2 0 6 3	37238603

## Problem D. Dumb Problem

Input file: *standard input*  
Output file: *standard output*  
Time limit: 1 second  
Memory limit: 1024 mebibytes

You are given an integer sequence of length  $n$ :  $a_1, a_2, \dots, a_n$ . You can perform the following operation exactly once:

- Choose a permutation  $p_1, p_2, \dots, p_n$  of  $1, 2, \dots, n$ .
- Then, for  $i$  from 1 to  $n$  in the natural order, execute:

$$a_{p_i} \leftarrow a_{p_i} + a_{p_i-1} + a_{p_i+1},$$

where  $a_0 = 0$  and  $a_{n+1} = 0$ .

Your goal is to maximize the sum of all elements in the sequence after the operation is completed.

### Input

The first line contains a single integer  $t$  ( $1 \leq t \leq 10^4$ ), the number of test cases. For each test case:

The first line contains an integer  $n$  ( $1 \leq n \leq 2 \cdot 10^5$ ).

The second line contains  $n$  integers  $a_1, a_2, \dots, a_n$  ( $-10^8 \leq a_i \leq 10^8$ ).

The sum of  $n$  does not exceed  $2 \cdot 10^5$ .

### Output

For each test case, output a single line with an integer representing the maximum possible sum of all elements in the sequence after performing the operation.

### Example

<i>standard input</i>	<i>standard output</i>
4	22
3	85
1 2 3	72
4	79
-1 3 7 6	
5	
4 1 0 5 2	
6	
4 -3 7 5 -9 3	

## Problem E. Bipartite Graph Weighting Problem

Input file: *standard input*  
Output file: *standard output*  
Time limit: 2 seconds  
Memory limit: 1024 mebibytes

You are given a bipartite graph. The left part contains  $n$  vertices, numbered from 1 to  $n$ , and the right part also contains  $n$  vertices, numbered from 1 to  $n$ . There are  $m$  edges, each connecting one vertex on the left to one vertex on the right.

You will be asked  $q$  independent queries. In each query, you are given three integers:  $(a, b, k)$ .

For a fixed query  $(a, b, k)$ , consider the following process on the given graph. Initially, every vertex (both left and right) has weight 0. You may perform the following operation any number of times:

- Choose an arbitrary subset  $S$  of the left vertices (possibly empty), and choose a positive real number  $p > 0$ .
- Let  $N(S)$  be the set of right vertices that are adjacent to at least one vertex in  $S$ .
- Increase the weight of every vertex in  $S$  by  $a \cdot p$ .
- Increase the weight of every vertex in  $N(S)$  by  $b \cdot p$ .

Let  $p_1, p_2, \dots, p_\ell$  be the values of  $p$  used in all your operations. These must satisfy

$$\sum_{i=1}^{\ell} p_i \leq 1.$$

Your goal is to choose the operations (the subsets  $S$  and the values  $p$ ) so that **the total sum of the weights of all vertices** (both left and right) is at most  $k$ . Under this constraint, you should maximize the total sum of the weights of all vertices of the left part.

For each query  $(a, b, k)$ , each time starting from all vertex weights equal to 0, compute the maximum possible total weight of the left part that can be obtained.

### Input

The first line contains a single integer  $t$  ( $1 \leq t \leq 1000$ ), the number of test cases. For each test case:

The first line contains three integers:  $n$ ,  $m$ , and  $q$  ( $1 \leq n \leq 2000$ ,  $0 \leq m \leq 10^4$ ,  $1 \leq q \leq 2 \cdot 10^5$ ).

Each of the next  $m$  lines contains two integers,  $u$  and  $v$  ( $1 \leq u, v \leq n$ ), denoting an edge between left vertex  $u$  and right vertex  $v$ .

Each of the next  $q$  lines contains three integers:  $a$ ,  $b$ , and  $k$  ( $0 \leq a, b \leq 10^6$ ,  $0 \leq k \leq 10^9$ ), describing a query.

There are no multiple edges. The sum of  $n$  does not exceed 2000. The sum of  $m$  does not exceed  $10^4$ . The sum of  $q$  does not exceed  $2 \cdot 10^5$ .

### Output

For each query, output a single real number: the maximum possible total sum of vertex weights of the left part that can be obtained for this query. Let your answer be  $a$  and the jury's answer be  $b$ . Your answer will be considered correct if  $\frac{|a-b|}{\max(1, |b|)} \leq 10^{-6}$ .

## Example

<i>standard input</i>	<i>standard output</i>
2	1.2500000000000000
5 8 3	1.3333333333333333
1 2	2.142857142857144
1 3	2.0000000000000000
2 4	0.0000000000000000
2 5	3.0000000000000000
3 1	
3 3	
4 2	
5 4	
1 3 5	
2 1 2	
5 2 3	
2 3 3	
1 2	
1 1	
2 1	
1 0 2	
0 2 2	
3 1 4	

## Problem F. Find the Circuit

Input file: *standard input*  
Output file: *standard output*  
Time limit: 4 seconds  
Memory limit: 1024 mebibytes

This is a communication problem. Your solution will be run twice on each test.

### First Run

You are given a connected undirected graph with  $n$  vertices and  $m$  edges. You are also given a special sequence of length  $k$  with vertex numbers  $p_1, \dots, p_k$  such that a simple cycle  $p_1 - p_2 - \dots - p_k - p_1$  exists in the graph. You must assign a direction to each edge of the graph.

### Second Run

Before the second run, the jury shuffles the labels of all vertices, and also shuffles the order of the edges that you output on the first run. You are given the resulting directed graph. Your task is to find the image of the cycle from the first run under this permutation: you must output the new labels of all the vertices on the cycle, starting from any vertex but maintaining their order.

### Input

The first line contains an integer  $op$  ( $op \in \{1, 2\}$ ), denoting the run number.

The second line contains two integers,  $n$  and  $m$  ( $3 \leq n \leq m \leq 5 \cdot 10^5$ ), the number of vertices and edges of the graph given to you. If  $op = 1$ , the graph is undirected; if  $op = 2$ , the graph is directed. The graph is connected and has no self-loops or multiple edges.

Each of the following  $m$  lines contains two integers,  $u$  and  $v$  ( $1 \leq u, v \leq n$ ), representing the edges in the graph. If the graph is directed, then the direction is  $u \rightarrow v$ .

If  $op = 1$ , the next line contains an integer  $k$  ( $3 \leq k \leq n$ ), the length of the cycle. The following line contains  $k$  integers  $p_1, \dots, p_k$ , the vertices on the cycle in order. This cycle exists in the graph given above: there are edges  $(p_1, p_2), (p_2, p_3), \dots, (p_k, p_1)$ .

### Output

If  $op = 1$ , you must assign a direction to each edge. Output  $m$  lines, each containing two integers  $u$  and  $v$ , denoting a directed edge  $u \rightarrow v$ . You may output the edges in any order, but you must output each edge from the input exactly once (with one of its two possible directions).

If  $op = 2$ , you must output the vertices of the cycle from the first run, using the shuffled labels and maintaining the cyclic order.

Note that your output should preserve the given cycle direction. For example, suppose the given sequence on the first run is 1 2 3 4, and after shuffling the vertex labels, it becomes 3 1 4 2. Then both outputs 3 1 4 2 and 4 2 3 1 will be accepted, as they represent cyclic shifts of the same directed cycle. On the other hand, output 2 4 1 3 will be rejected, since it corresponds to the reversed direction.

## Examples

<i>standard input</i>	<i>standard output</i>
1 5 6 1 2 2 5 2 3 3 4 3 5 4 5 4 2 3 4 5	2 3 3 4 5 2 3 5 4 5 1 2
2 5 6 3 5 2 1 4 5 5 2 2 4 1 4	1 4 5 2

## Note

The examples show two runs of a particular solution on the example. After the first run, the labels of vertices 1, 2, 3, 4, 5 are permuted into 3, 5, 2, 1, 4. When your solution is checked, the permutation may be different.

## Problem G. Watering System

Input file: *standard input*  
Output file: *standard output*  
Time limit: 2 seconds  
Memory limit: 1024 mebibytes

There are  $n$  flower pots in a row, numbered from 1 to  $n$ . Along the row, you can place watering machines. Each watering machine is characterized by its position  $x$  (an integer between 1 and  $n$ ) and its direction: left or right.

All watering machines share the same watering range  $L$  (a non-negative integer).

- A watering machine at position  $x$  pointing to the right waters all pots with indices in the segment  $[x, x + L]$ .
- A watering machine at position  $x$  pointing to the left waters all pots with indices in the segment  $[x - L, x]$ .

Only pots with indices between 1 and  $n$  exist.

Initially, there are no watering machines. You need to process  $q$  operations of two types:

- **Insert a watering machine.** An operation of the form “1  $d$   $x$ ” inserts a new watering machine at position  $x$ .  
If  $d = 0$ , the watering machine points to the left.  
If  $d = 1$ , the watering machine points to the right.  
Multiple watering machines may be placed at the same position. Operations are given in chronological order, and there are no deletions.
- **Range query.** An operation of the form “2  $\ell$   $r$ ” asks the following question:  
Consider the current set of watering machines. Suppose all watering machines have the same range  $L$ . Find the smallest integer  $L \geq 0$  such that every pot with index in the segment  $[\ell, r]$  is watered by at least one watering machine. Note that watering machines outside the interval  $[\ell, r]$  may help water pots inside  $[\ell, r]$ . If there is no integer  $L$  that makes all pots in  $[\ell, r]$  watered (no matter how large  $L$  is), you must output  $-1$  for this query.

### Input

The first line contains two integers,  $n$  and  $q$  ( $1 \leq n, q \leq 3 \cdot 10^5$ ), representing the number of pots and the number of operations.

Each of the next  $q$  lines describes one operation in the order they must be processed:

- “1  $d$   $x$ ”: insert a watering machine at position  $x$  with direction  $d$ , ( $d \in \{0, 1\}$ ,  $1 \leq x \leq n$ ). Here,  $d = 0$  means the watering machine points to the left, and  $d = 1$  means it points to the right.
- “2  $\ell$   $r$ ”: query the minimal range  $L$  for the segment  $[\ell, r]$  ( $1 \leq \ell \leq r \leq n$ ).

### Output

For each query of the form “2  $\ell$   $r$ ”, output a single line with one integer:

- the minimal integer  $L \geq 0$  such that every pot in  $[\ell, r]$  is watered, or
- $-1$  if it is impossible.

## Example

<i>standard input</i>	<i>standard output</i>
10 11	-1
1 0 6	7
2 5 8	6
1 1 3	5
2 9 10	5
2 3 9	4
1 1 8	4
2 1 9	
2 1 8	
1 0 4	
2 3 7	
2 2 9	

## Problem H. Longest Common Prefix

Input file: *standard input*  
Output file: *standard output*  
Time limit: 1 second  
Memory limit: 1024 mebibytes

You are given a string  $s$  of length  $n$ .

For each position  $i$  where  $1 \leq i \leq n$ , let  $t_i$  be the string obtained from  $s$  by deleting the  $i$ -th character of  $s$  (and keeping the relative order of all other characters).

For two strings  $x$  and  $y$ , let  $\text{lcp}(x, y)$  denote the *length* of their longest common prefix, that is, the largest integer  $\ell \geq 0$  such that the first  $\ell$  characters of  $x$  and  $y$  are equal (if  $x_1 = y_1, x_2 = y_2, \dots, x_\ell = y_\ell$ ).

Your task is to choose two **different** positions  $i$  and  $j$  such that the value  $\text{lcp}(t_i, t_j)$  is as large as possible, and compute this maximum possible value.

Formally, you need to find

$$\max_{1 \leq i < j \leq n} \text{lcp}(t_i, t_j).$$

You do not need to output  $i$  or  $j$ , only the maximum value of  $\text{lcp}(t_i, t_j)$ .

### Input

The first line contains a single integer  $t$  ( $1 \leq t \leq 2 \cdot 10^5$ ), the number of test cases. For each test case:

A single line contains a string  $s$  that consists of lowercase English letters ( $2 \leq |s| \leq 5 \cdot 10^5$ ).

The sum of  $|s|$  does not exceed  $5 \cdot 10^5$ .

### Output

For each test case, output a single integer on a separate line, representing the maximum possible value of  $\text{lcp}(t_i, t_j)$  over all pairs of indices  $i \neq j$ .

### Example

<i>standard input</i>	<i>standard output</i>
5	2
abac	4
abbbb	3
cbacb	4
babcc	1
aa	

## Problem I. DFS Order: Extra Stage

Input file: *standard input*  
Output file: *standard output*  
Time limit: 3 seconds  
Memory limit: 1024 mebibytes

You are given  $m$  depth-first search (DFS) orders of an unknown rooted tree.

We consider rooted trees with  $n$  vertices labeled from 1 to  $n$ , where vertex 1 is the root. The tree is undirected and connected, and has exactly  $n - 1$  edges.

**DFS definition.** For a fixed rooted tree, a DFS order is obtained as follows:

- All vertices are initially unvisited.
- Start at the root 1, mark it as visited and **output** it.
- When you are at some vertex  $v$ , consider all children of  $v$  in the rooted tree. Choose its children in **any** order. For each chosen child  $u$  that is still unvisited, go to  $u$ , mark it as visited, output  $u$ , and continue the DFS from  $u$  in the same way.

For a fixed tree, different choices of the order in which the children of each vertex are processed may produce different DFS orders. All DFS orders are permutations of  $1, 2, \dots, n$  and always start with 1.

You are given  $m$  permutations of  $1, 2, \dots, n$ , each starting with 1. You are told that each of them is a DFS order of the **same** rooted tree (with root 1) in the sense defined above (possibly using different choices of child orders for different DFS runs).

Your task is to determine how many different rooted trees could produce **all** of these  $m$  DFS orders.

Two rooted trees are considered different if their sets of edges are different.

Because the answer can be very large, you should output it modulo  $10^9 + 7$ .

### Input

The first line contains two integers  $n$  and  $m$  ( $1 \leq n, m \leq 500$ ).

Each of the next  $m$  lines contains a permutation  $p_{k,1}, p_{k,2}, \dots, p_{k,n}$  of the integers  $1, 2, \dots, n$ , describing the  $k$ -th DFS order.

For every  $k$ , all  $p_{k,i}$  are distinct and  $p_{k,1} = 1$ .

### Output

Output a single integer: the number of rooted trees with vertex set  $1, 2, \dots, n$  and root 1 for which **every** given sequence is a valid DFS order of that tree, taken modulo  $10^9 + 7$ .

### Examples

<i>standard input</i>	<i>standard output</i>
3 2 1 2 3 1 3 2	1
4 1 1 2 3 4	5
5 2 1 2 3 4 5 1 2 4 3 5	3

## Problem J. Re: Becoming the Programming Champion

Input file: *standard input*  
Output file: *standard output*  
Time limit: 1 second  
Memory limit: 1024 mebibytes

You and your two teammates are participating in a programming contest, but due to the final exams, you all have to leave early. Each of you has a specific departure time  $\ell_i$  (the time in minutes after the contest starts when you must leave). After the contest, you review the solutions and realize that each problem is perfectly suited for one of you: problem  $i$  is best solved by person  $p_i$ , who can complete it in  $c_i$  minutes without any wrong submissions. Unfortunately, due to the pressure of exams, you didn't perform well in the original contest.

In a dream, you see the champion team from the live broadcast: they solved all  $n$  problems with a total penalty time  $t$ . When you wake up, you discover you've been reborn on the morning of the contest day. Now, with perfect memory of all problem details and the champion's performance, you want to determine if there's a way to beat them this time.

The contest rules state:

- Only one computer is available, so problems must be solved sequentially (one after another).
- Each problem  $i$  must be assigned to person  $p_i$ , who must start solving it before their departure time  $\ell_{p_i}$ .
- If person  $p_i$  starts solving problem  $i$  at time  $s$ , they must finish by  $s + c_i \leq \ell_{p_i}$ .
- The total penalty time is the sum of the completion times for all solved problems.

Given  $n$ ,  $t$ , and the parameters  $p_i$  and  $c_i$  for each problem, determine if there exists an order of solving the problems such that:

- All  $n$  problems are solved.
- The total penalty time is **strictly less** than  $t$ .

If such an arrangement exists, output "YES"; otherwise, output "NO".

### Input

The first line contains a single integer  $q$  ( $1 \leq q \leq 10^5$ ), the number of test cases. For each test case:

The first line contains four integers:  $n$ ,  $\ell_1$ ,  $\ell_2$ , and  $\ell_3$  ( $1 \leq n \leq 10^5$ ,  $1 \leq \ell_1, \ell_2, \ell_3 \leq 3 \cdot 10^7$ ), representing the number of problems and the departure times (in minutes after contest start) of the three teammates.

Each of the following  $n$  lines contains two integers,  $p_i$  and  $c_i$  ( $1 \leq p_i \leq 3$ ,  $1 \leq c_i \leq 300$ ), where  $p_i$  denotes the designated teammate for problem  $i$ , and  $c_i$  is the required time (in minutes) for them to complete it.

The last line contains a single integer  $t$  ( $1 \leq t \leq 10^{13}$ ), representing the total penalty time of the champion team.

The sum of  $n$  over all test cases does not exceed  $10^5$ .

### Output

For each test case, if there exists an order of solving problems that satisfies the constraints (all problems solved, penalty strictly less than  $t$ ), output "YES"; otherwise, output "NO".

## Examples

<i>standard input</i>	<i>standard output</i>
2 3 100 150 175 1 100 2 25 3 50 401 5 100 200 300 1 30 1 30 1 40 2 110 3 50 1275	YES NO
1 1 100 300 300 1 300 300	NO

## Problem K. Cyclic Shift

Input file: *standard input*  
Output file: *standard output*  
Time limit: 1 second  
Memory limit: 1024 mebibytes

You are given a sequence of  $n$  integers:  $a_1, a_2, \dots, a_n$ .

Consider all  $n$  possible cyclic shifts (rotations) of this sequence. For a starting position  $p$  ( $1 \leq p \leq n$ ), the corresponding cyclic shift is the sequence

$$b_1, b_2, \dots, b_n = a_p, a_{p+1}, \dots, a_n, a_1, a_2, \dots, a_{p-1}.$$

For this shifted sequence, define its **prefix maximum sequence**  $c_1, c_2, \dots, c_n$  as

$$c_i = \max(b_1, b_2, \dots, b_i) \text{ for all } i = 1, 2, \dots, n.$$

We compare two sequences of the same length by the usual lexicographical order:  $c$  is lexicographically smaller than  $d$  if and only if there exists an index  $i$  such that  $c_1 = d_1, c_2 = d_2, \dots, c_{i-1} = d_{i-1}$ , and  $c_i < d_i$ .

Your task is to choose a cyclic shift of the original sequence such that its prefix maximum sequence is the lexicographically smallest among all  $n$  possible cyclic shifts.

### Input

The first line contains a single integer  $t$  ( $1 \leq t \leq 2 \cdot 10^5$ ), the number of test cases. For each test case:

The first line contains a single integer  $n$  ( $1 \leq n \leq 5 \cdot 10^5$ ).

The second line contains  $n$  integers  $a_1, a_2, \dots, a_n$  ( $1 \leq a_i \leq n$ ).

The sum of  $n$  over all test cases does not exceed  $5 \cdot 10^5$ .

### Output

For each test case, output one line containing  $n$  integers: the lexicographically smallest prefix maximum sequence after a cyclic shift.

### Example

<i>standard input</i>	<i>standard output</i>
6	1 5 5 5 5
5	1 3 3 3
5 4 3 2 1	1 1 2 2 3
4	1 1 2 3 3
1 3 1 3	1 2 2 3 3 4
5	1 2 2 3 3 4
1 2 1 3 1	
5	
2 3 2 1 1	
6	
1 2 1 3 1 4	
6	
2 1 3 1 4 1	

## Problem L. Cyclic Shift II

Input file: *standard input*  
Output file: *standard output*  
Time limit: 2 seconds  
Memory limit: 1024 mebibytes

You are given two integer sequences  $A$  and  $B$  of lengths  $2n$  and  $2m$ , respectively. All elements are non-zero integers.

The sequence  $A = (a_1, a_2, \dots, a_{2n})$  satisfies the following condition: for every integer  $i$  such that  $1 \leq i \leq n$ , there are exactly two indices  $j$  such that  $|a_j| = i$ . In particular,  $\{|a_j| : 1 \leq j \leq 2n\} = \{1, 2, \dots, n\}$ , and each absolute value appears exactly twice (if we disregard the signs).

The sequence  $B = (b_1, b_2, \dots, b_{2m})$  satisfies a similar condition: for every  $i$  such that  $1 \leq i \leq m$ , there are exactly two indices  $j$  such that  $|b_j| = i$ .

You may perform the following operations on the sequence  $A$ , in any order and any number of times:

1. **Cyclic shift.** Regard the current sequence as a cycle, and perform a rotation:

$$(a_1, a_2, \dots, a_{2k}) \longrightarrow (a_{r+1}, a_{r+2}, \dots, a_{2k}, a_1, \dots, a_r)$$

where  $0 \leq r < 2k$ .

2. **Delete a prefix of a pair of opposite numbers.** If the current sequence has the form  $A = (x, -x, S_1)$ , where  $x \neq 0$  and  $S_1$  may be empty, you may replace  $A$  by  $S_1$ ; that is, delete the first two elements,  $x$  and  $-x$ .
3. **Insert a new pair of opposite numbers at the front.** If the current sequence is  $A = (S_1)$  (may be empty), you may replace it by  $(x, -x, S_1)$ , where  $x \neq 0$ , and neither  $x$  nor  $-x$  appears anywhere in  $S_1$ .
4. **Reverse and negate.** If the current sequence is

$$A = (a_1, a_2, \dots, a_{2k}),$$

you may replace it by

$$\text{nRev}(A) = (-a_{2k}, -a_{2k-1}, \dots, -a_1).$$

5. **Rearrange across a cut.** Choose a cut that splits the current sequence into a prefix and a suffix. Suppose the sequence can be written as

$$A = (S_1, x, S_2, S_3, y, S_4)$$

where  $x > 0$ ,  $y \in \{x, -x\}$ , and the cut is between  $S_2$  and  $S_3$ . Here,  $S_1$ ,  $S_2$ ,  $S_3$ , and  $S_4$  may be empty sequences. Then you may apply one of the following transformations:

- If  $y = x$  (that is, you choose a pair  $x$  and  $x$ ), you may replace  $A$  by

$$(S_1, \text{nRev}(S_3), x, \text{nRev}(S_4), S_2, y).$$

- If  $y = -x$  (that is, you choose a pair  $x$  and  $-x$ ), you may replace  $A$  by

$$(S_1, S_4, x, S_3, S_2, y).$$

You have to determine if it is possible to transform sequence  $A$  into a sequence that is *equivalent* to sequence  $B$  by applying these operations a finite number of times.

Let  $C = (c_1, \dots, c_{2k})$  and  $D = (d_1, \dots, d_{2k})$  be two integer sequences of the same length. We say that  $C$  and  $D$  are *equivalent* if and only if there exists a mapping  $f : \mathbb{Z} \rightarrow \mathbb{Z}$  such that:

- for every integer  $x$ ,  $f(-x) = -f(x)$ ,
- whenever  $f(x) \neq 0$ , the integers  $x$  and  $f(x)$  have the same sign (both positive or both negative),

and for all  $1 \leq i \leq 2k$  we have  $d_i = f(c_i)$ . In other words, if we replace each element  $c_i$  of the sequence  $C$  by  $f(c_i)$ , we obtain the sequence  $D$ . The values of  $f$  on integers that do not occur in the sequences may be chosen arbitrarily.

## Input

The first line contains a single integer  $t$  ( $1 \leq t \leq 10^5$ ), the number of test cases. For each test case:

The first line contains an integer  $n$  ( $1 \leq n \leq 5 \cdot 10^5$ ), denoting that the length of sequence  $A$  is  $2n$ .

The second line contains  $2n$  integers, denoting  $a_1, a_2, \dots, a_{2n}$ .

The third line contains an integer  $m$  ( $1 \leq m \leq 5 \cdot 10^5$ ), denoting that the length of sequence  $B$  is  $2m$ .

The fourth line contains  $2m$  integers, denoting  $b_1, b_2, \dots, b_{2m}$ .

The sequences  $A$  and  $B$  meet the requirements in the statement.

The total size of all test cases is bounded by  $\sum n + \sum m \leq 10^6$ .

## Output

For each test case, if it is possible to make  $A$  equivalent to  $B$ , output “YES”; otherwise, output “NO”.

## Examples

<i>standard input</i>	<i>standard output</i>
4 1 1 -1 2 -1 -2 2 1 1 1 1 1 -1 1 4 1 2 -1 3 -4 2 3 -4 4 1 2 -1 -2 4 3 4 3 4 4 3 -1 -2 -3 2 1 -4 3 -1 1 3 -3 2 2	YES NO YES NO
5 4 1 2 -3 -2 4 -1 3 -4 6 -3 5 2 3 -2 -5 1 -6 -4 -1 4 6 5 -2 4 -4 3 2 -1 -5 1 -3 5 5 3 -4 1 -5 4 -1 2 -2 -3 5 4 -2 1 4 2 -4 3 -1 -3 5 -1 -5 -2 2 1 -4 -3 3 4 5 3 2 -1 -1 -3 -2 3 4 -4 -2 -1 4 1 -2 3 -3 5 3 5 -5 -2 2 -1 -3 -4 1 4 5 3 5 -2 -5 -1 2 -4 1 4 -3	YES YES NO YES NO

## Note

In the first example:

In the first test case,  $(1, -1) \xrightarrow{op\ 3} (-2, 2, 1, -1) \xrightarrow{op\ 1} (-1, -2, 2, 1)$ .

In the third test case, suppose  $x = 3$ ,  $y = 3$ ,  $S_1 = (1, 2, -1)$ ,  $S_3 = (-4, 2)$ ,  $S_4 = (-4)$ , and  $S_2$  is empty.

Then  $A = (S_1, x, S_2, S_3, y, S_4)$ , and  $A \xrightarrow{op\ 5} (1, 2, -1, -2, 4, 3, 4, 3)$ .