



## Problem K. Reverse KMP

Time limit: 1 second  
Memory limit: 256 megabytes

In the KMP algorithm, the next array (also known as the LPS array, for Longest Prefix Suffix, or the failure function) is a core concept. Given a string  $S = s_1s_2\dots s_n$  of length  $n$ , its next array  $\text{next}[1..n]$  is defined such that  $\text{next}[i]$  represents the length of the longest equal proper prefix and proper suffix of the substring  $S[1..i]$ , specifically,  $\text{next}[1] = 0$ . Formally, it is defined as:

$$\text{next}[i] = \max_{k=0,\dots,i-1} \{k : S[1\dots k] = S[i-k+1\dots i]\}$$

Here,  $S[l..r]$  is defined as the substring formed by the  $l$ -th character to the  $r$ -th character of the string  $S$ . It is considered that  $\forall 1 \leq i \leq n, S[1..0] = S[i+1..i]$ , both of which are empty strings.

Given an array  $A[1..n]$  of length  $n$ . You need to count how many different strings  $S$  of length  $n$  defined over the character set  $\Sigma$  have a next array that is exactly equal to the given array  $A$ . The size of the character set is  $m$ . Output the number of such strings modulo 998 244 353.

### Input

There are multiple test cases in a single test file. The first line of the input contains a single integer  $T$  ( $1 \leq T \leq 10^5$ ), indicating the number of test cases.

For each test case:

- The first line contains two integers  $n$  ( $2 \leq n \leq 10^5$ ) and  $m$  ( $1 \leq m \leq 10^6$ ) representing the length of the given array and the size of the character set.
- The second line contains  $n$  integers, separated by spaces, representing the given array  $A$ . It is guaranteed that  $\forall 1 \leq i \leq n, 0 \leq A_i \leq i - 1$ .

It is guaranteed that the total sum of  $n$  does not exceed  $5 \times 10^5$ , i.e.,  $\sum n \leq 5 \times 10^5$ .

### Output

For each test case, output a single line with a single integer, representing the number of strings that satisfy the conditions, with the answer taken modulo 998 244 353.

### Example

standard input	standard output
3	3
3 3	24
0 1 2	0
7 3	
0 0 0 1 2 3 0	
7 3	
0 0 0 1 2 3 1	

### Note

For the second group of data in the sample, let us assume the character set  $\Sigma = \{ 'a', 'b', 'c' \}$ . The 24 strings that meet the requirements are:

abbabbb abbabbc abcabcb abcabcc acbacbb acbacbc  
accaccb accacc baabaaa baabaac bacbaca bacbacc  
bcabcaa bcabcac bccbca bccbcc caacaaa caacaab  
cabcaba cabcabb cbacbaa cbacbab cbbcbbba cbbcbbb