

# I – Palindromes

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Memory limit: 1024 MB  
Time limit: 3 s

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In this problem we consider strings over the binary alphabet  $\{a, b\}$ . A string is called a *palindrome* if it reads the same from left to right and from right to left. For example, the strings **a**, **aba**, and **babbab** are palindromes, but **abab** is not.

There is an unknown binary string  $s$  of length  $N$  over the alphabet  $\{a, b\}$ . We only know that its prefixes (that is, initial fragments) of lengths  $a_1, \dots, a_n$  are palindromes. In how many ways can the string  $s$  be recovered? The answer can be quite large; it suffices to return its remainder modulo  $m$ .

Note that the sought string  $s$  may have other prefixes being palindromes, in addition to the ones of lengths  $a_1, \dots, a_n$ .

## Input

The first line contains three integers  $N$ ,  $n$ , and  $m$  ( $1 \leq N \leq 10^{18}$ ,  $1 \leq n \leq 500\,000$ ,  $2 \leq m \leq 10^9$ ) that represent the length of the string, the number of palindromic prefixes of the string, and the number used to compute the result.

The second line contains a strictly increasing sequence of  $n$  integers  $a_1, a_2, \dots, a_n$  (with  $1 \leq a_i \leq N$ ) that denote the lengths of the palindromic prefixes of the sought string.

## Output

The output should contain one non-negative integer, the number of strings of length  $N$  that have a palindromic prefix of each length  $a_1, \dots, a_n$ , modulo  $m$ .

## Example

For the input data:

```
10 3 100
2 5 9
```

the correct result is:

```
8
```

**Explanation:** There are 8 strings of length 10 whose prefixes of lengths 2, 5, and 9 are palindromes:

1. aaaaaaaaaa
2. aaaaaaaaaab
3. aabaaabaaa
4. aabaaabaab
5. bbabbbabba
6. bbabbbabbb
7. bbbbbbbbbb
8. bbbbbbbbbb